

Electricity and MagnetismOBJECTIVE QUESTIONSIT-JAM-2005

Q1. A small loop of wire of area $A = 0.01 \text{ m}^2$, $N = 40$ turns and resistance $R = 20 \Omega$ is initially kept in a uniform magnetic field B in such a way that the field is normal to the loop. When it is pulled out of the magnetic field, a total charge of $Q = 2 \times 10^{-5} \text{ C}$ flows through the coil. The magnetic of the field B is

- (a) $1 \times 10^{-3} \text{ T}$ (b) $4 \times 10^{-3} \text{ T}$
 (c) zero (d) unobtainable, as the data is insufficient

Ans.: (a)

Solution: Magnetic flux through the loop $\phi = NBA$

$$\text{Induced e.m.f } \varepsilon = -\frac{d\phi}{dt} \text{ and induced current } i = -\frac{1}{R} \frac{d\phi}{dt} = \frac{dQ}{dt} \Rightarrow -\frac{1}{R} d\phi = dQ.$$

$$\text{Thus } \frac{1}{20} \times (40 \times B \times 0.01) = 2 \times 10^{-5} \Rightarrow B = 1 \times 10^{-3} \text{ T}.$$

Q2. Two point charges $+q_1$ and $+q_2$ are fixed with a finite distance d between them. It is desired to put a third charge q_3 in between these two charges on the line joining them so that the charge q_3 is in equilibrium. This is

- (a) possible only if q_3 is positive
 (b) possible only if q_3 is negative
 (c) possible irrespective of the sign of q_3
 (d) not possible at all

Ans.: (c)

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IIT-JAM-2006

Q3. Two electric dipoles P_1 and P_2 are placed at $(0,0,0)$ and $(1,0,0)$ respectively with both of them pointing in the $+z$ direction. Without changing the orientations of the dipoles P_2 is moved to $(0,2,0)$. The ratio of the electrostatic potential energy of the dipoles after moving to that before moving is

- (a) $\frac{1}{16}$ (b) $\frac{1}{2}$ (c) $\frac{1}{4}$ (d) $\frac{1}{8}$

Ans: (d)

Solution: Electrostatic potential energy $U \propto \frac{1}{r^3} \Rightarrow \frac{U_2}{U_1} = \frac{r_1^3}{r_2^3} = \frac{1}{8}$

Q4. A small magnetic dipole is kept at the origin in the x - y plane. One wire L_1 is located at $z = -a$ in the x - z plane with a current I flowing in the positive x direction. Another wire L_2 is at $z = +a$ in y - z plane with the same current I as in L_1 , flowing in the positive y -direction. The angle ϕ made by the magnetic dipole with respect to the positive x -axis is

- (a) 225° (b) 120° (c) 45° (d) 270°

Ans.: (a)

Solution: Magnetic field at $z = 0$ due to wire at $z = -a$ is $\vec{B} = -B\hat{y}$.

Magnetic field at $z = 0$ due to wire at $z = +a$ is $\vec{B} = -B\hat{x}$.

Resultant magnetic field at $z = 0$ makes an angle of 45° with $-\hat{x}$ and 225° with \hat{x} .

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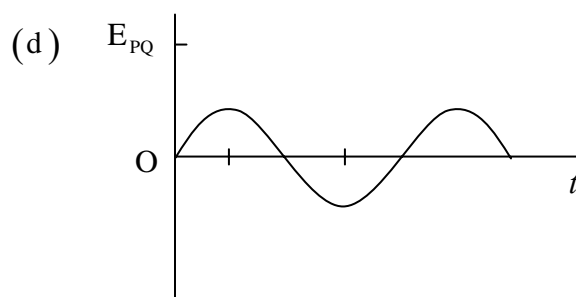
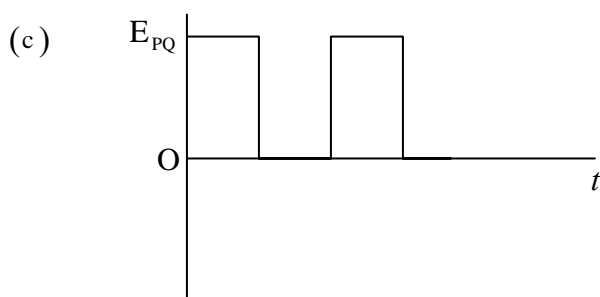
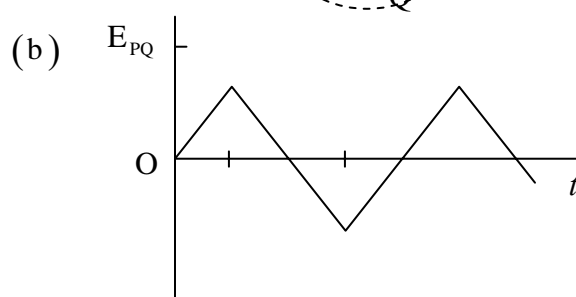
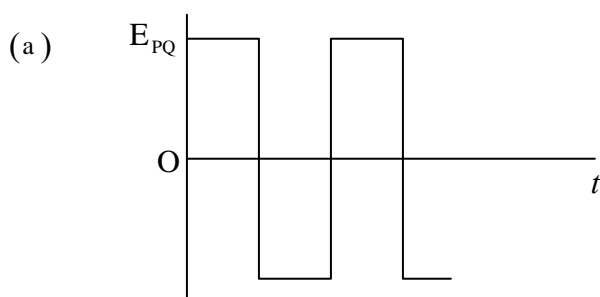
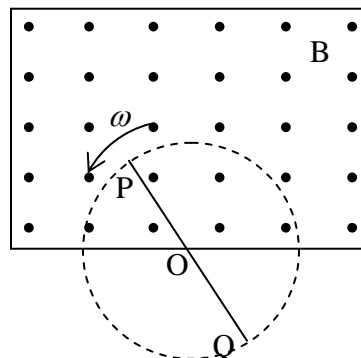
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IIT-JAM-2007

Q5. A uniform and constant magnetic field B coming out of the plane of the paper exists in a rectangular region as shown in the figure. A conducting rod PQ is rotated about O with a uniform angular speed ω in the plane of the paper. The emf E_{PQ} induced between P and B is best represented by the graph



Ans.: (a)

IIT-JAM-2008

Q6. If the electrostatic potential at a point (x, y) is given by $V = (2x + 4y)$ volts, the electrostatic energy density at that point (in J/m^3) is

- (a) $5\epsilon_0$ (b) $10\epsilon_0$ (c) $20\epsilon_0$ (d) $\frac{1}{2}\epsilon_0(2x + 4y)^2$

Ans.: (a)

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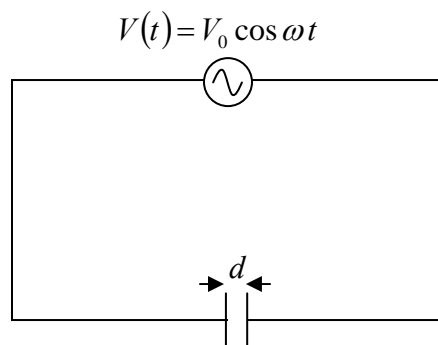
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Solution: $\vec{E} = -\vec{\nabla}V = -2\hat{x} - 4\hat{y} \Rightarrow |\vec{E}| = 20 \text{ V/m}$

$$\text{Electrostatic energy density} = \frac{1}{2} \epsilon_0 |\vec{E}|^2 = \frac{1}{2} \epsilon_0 \times 20 = 10 \epsilon_0 \text{ J/m}^3$$

IIT-JAM-2009

Q7. An oscillating voltage $V(t) = V_0 \cos \omega t$ is applied across a parallel plate capacitor having a plate separation d . The displacement current density through the capacitor is



(a) $\frac{\epsilon_0 \omega V_0 \cos \omega t}{d}$

(b) $\frac{\epsilon_0 \mu_0 \omega V_0 \cos \omega t}{d}$

(c) $-\frac{\epsilon_0 \mu_0 \omega V_0 \cos \omega t}{d}$

(d) $-\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Ans.: (d)

Solution: Displacement current density $J_d = \epsilon_0 \frac{\partial E}{\partial t} = \frac{\epsilon_0}{d} \frac{\partial V(t)}{\partial t} = -\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Q8. An electric field $\vec{E}(\vec{r}) = (\alpha \hat{r} + \beta \sin \theta \cos \phi \hat{\phi})$ exists in space. What will be the total charge enclosed in a sphere of unit radius centered at the origin?

(a) $4\pi\epsilon_0\alpha$

(b) $4\pi\epsilon_0(\alpha + \beta)$

(c) $4\pi\epsilon_0(\alpha - \beta)$

(d) $4\pi\epsilon_0\beta$

Ans.: (a)

Solution: $Q_{enc} = \epsilon_0 \oint \vec{E} \cdot d\vec{a} = \epsilon_0 \int (\alpha \hat{r} + \beta \sin \theta \cos \phi \hat{\phi}) \cdot (r^2 \sin \theta d\theta d\phi \hat{r}) = 4\pi\alpha\epsilon_0$

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IIT-JAM-2010

Q9. The magnetic field associated with the electric field vector $\vec{E} = E_0 \sin(kz - \omega t)\hat{j}$ is given by

(a) $\vec{B} = -\frac{E_0}{c} \sin(kz - \omega t)\hat{i}$

(b) $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{i}$

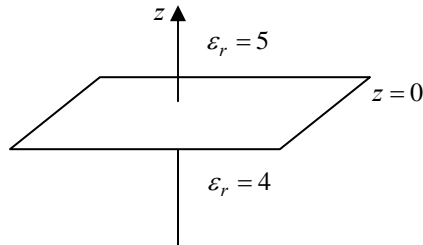
(c) $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{j}$

(d) $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{k}$

Ans.: (a)

Solution: $\vec{B} = \frac{\vec{k} \times \vec{E}}{\omega} = \frac{k\hat{z} \times E_0 \sin(kz - \omega t)\hat{j}}{\omega} = -\frac{kE_0}{\omega} \sin(kz - \omega t)\hat{x} = -\frac{E_0}{c} \sin(kz - \omega t)\hat{x}$

Q10. Assume that $z = 0$ plane is the interface between two linear and homogenous dielectrics (see figure). The relative permittivities are $\epsilon_r = 5$ for $z > 0$ and $\epsilon_r = 4$ for $z < 0$. The electric field in the region $z > 0$ is $\vec{E}_1 = (3\hat{i} - 5\hat{j} + 4\hat{k})kV/m$. If there are no free charges on the interface, the electric field in the region $z < 0$ is given by



(a) $\vec{E}_2 = \left(\frac{3}{4}\hat{i} - \frac{5}{4}\hat{j} + \hat{k}\right)kV/m$

(b) $\vec{E}_2 = (3\hat{i} - 5\hat{j} + \hat{k})kV/m$

(c) $\vec{E}_2 = (3\hat{i} - 5\hat{j} - 5\hat{k})kV/m$

(d) $\vec{E}_2 = (3\hat{i} - 5\hat{j} + 5\hat{k})kV/m$

Ans.: (d)

Solution: $\because E_1^\perp = E_2^\perp \Rightarrow E_2^\perp = 3\hat{i} - 5\hat{j}$

and $\sigma_f = 0 \Rightarrow D_1^\perp = D_2^\perp \Rightarrow E_2^\perp = \frac{\epsilon_1}{\epsilon_2} E_1^\perp = \frac{5}{4}(3\hat{i} - 5\hat{j}) = 3.75\hat{i} - 6.25\hat{j}$

$\Rightarrow \vec{E}_2 = (3\hat{i} - 5\hat{j} + 5\hat{k})kV/m$

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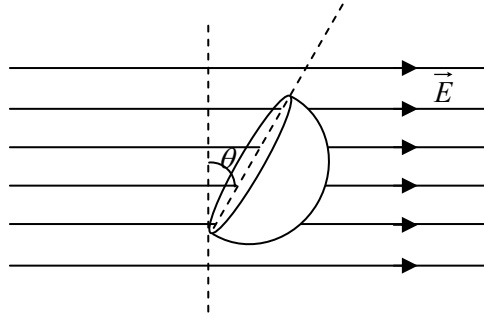
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Q11. A closed Gaussian surface consisting of a hemisphere and a circular disc of radius R , is placed in a uniform electric field \vec{E} , as shown in the figure. The circular disc makes an angle $\theta = 30^\circ$ with the vertical. The flux of the electric field vector coming out of the curved surface of the hemisphere is

- (a) $\frac{1}{2} \pi R^2 E$
 (b) $\frac{\sqrt{3}}{2} \pi R^2 E$
 (c) $\pi R^2 E$
 (d) $2\pi R^2 E$



Ans.: (b)

Solution: $\vec{E} = E \cos 30^\circ \hat{z} + E \sin 30^\circ \hat{x} = \frac{\sqrt{3}}{2} E \hat{z} + \frac{1}{2} E \hat{x}$

$$\phi_E = \int_S \vec{E} \cdot d\vec{a} = \int \int \left(\frac{\sqrt{3}}{2} E \hat{z} + \frac{1}{2} E \hat{x} \right) \cdot (R^2 \sin \theta d\theta d\phi \hat{r})$$

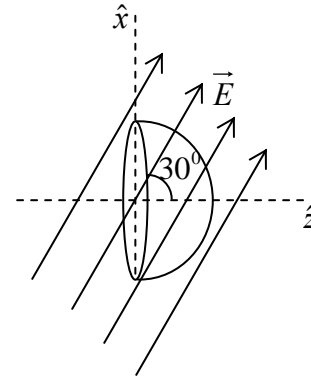
$$\phi_E = R^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} \left(\frac{\sqrt{3}}{2} E \cos \theta + \frac{1}{2} E \sin \theta \cos \phi \right) (\sin \theta d\theta d\phi)$$

$$\phi_E = \frac{\sqrt{3}}{2} ER^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} (\cos \theta \sin \theta) d\theta d\phi + \frac{1}{2} ER^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} (\sin^2 \theta \cos \phi) d\theta d\phi$$

$$\phi_E = \frac{\sqrt{3}}{2} ER^2 \times 2\pi \times \frac{1}{2} + 0 = \frac{\sqrt{3}}{2} \pi R^2 E$$

OR

$$\phi_E = \int_S \vec{E} \cdot d\vec{a} = E \cos 30^\circ \times \pi R^2 = \frac{\sqrt{3}}{2} \pi R^2 E$$



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IIT-JAM-2011

Q12. Equipotential surface corresponding to a particular charge distribution are given by $4x^2 + (y-2)^2 + z^2 = V_i$ where the values of V_i are constants. The electric field \vec{E} at the origin is

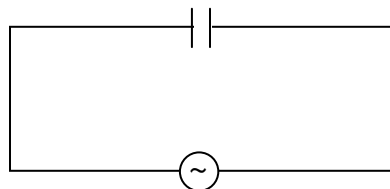
- (a) $\vec{E} = 0$ (b) $\vec{E} = 2\hat{x}$ (c) $\vec{E} = 4\hat{y}$ (d) $\vec{E} = -4\hat{y}$

Ans.: (d)

Solution: $\vec{E} = -\nabla V = 8x\hat{x} + 2(y-2)\hat{y} + 2z\hat{z} \Rightarrow \vec{E}(0,0) = -4\hat{y}$

IIT-JAM-2012

Q13. A parallel plate air-gap capacitor is made up of two plates of area 10 cm^2 each kept at a distance of 0.88 mm . A sine wave of amplitude 10 V and frequency 50 Hz is applied across the capacitor as shown in the figure. The amplitude of the displacement current density (in mA/m^2) between the plates will be closest to



- (a) 0.03 (b) 0.30 (c) 3.00 (d) 30.00

Ans.: (a)

Solution: Displacement current density $J_d = \epsilon_0 \frac{\partial E}{\partial t} = \frac{\epsilon_0}{d} \frac{\partial V(t)}{\partial t} = -\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Amplitude of the displacement current density (in mA/m^2) $J_{0d} = \frac{\epsilon_0 \omega V_0}{d} = \frac{2\pi\epsilon_0 f V_0}{d}$

$$\Rightarrow J_{0d} = 4\pi\epsilon_0 \frac{fV_0}{2d} = \frac{1}{9 \times 10^9} \frac{50 \times 10}{2 \times 88 \times 10^{-5}} = 0.03 \text{ mA/m}^2$$

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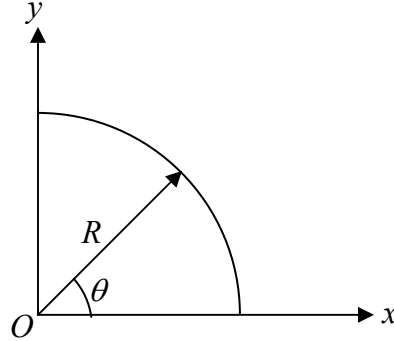
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Q14. A segment of a circular wire of radius R , extending from $\theta = 0$ to $\pi/2$, carries a constant linear charge density λ . The electric field at origin O is

- (a) $\frac{\lambda}{4\pi\epsilon_0 R}(-\hat{x} - \hat{y})$
 (b) $\frac{\lambda}{4\pi\epsilon_0 R}\left(-\frac{1}{\sqrt{2}}\hat{x} - \frac{1}{\sqrt{2}}\hat{y}\right)$
 (c) $\frac{\lambda}{4\pi\epsilon_0 R}\left(-\frac{1}{2}\hat{x} - \frac{1}{2}\hat{y}\right)$
 (d) 0



Ans.: (a)

Solution: $\vec{E} = -E_x\hat{x} - E_y\hat{y}$

where $E_x = \int_{line} dE \cos \theta$, $E_y = \int_{line} dE \sin \theta$.

and $dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2}$.

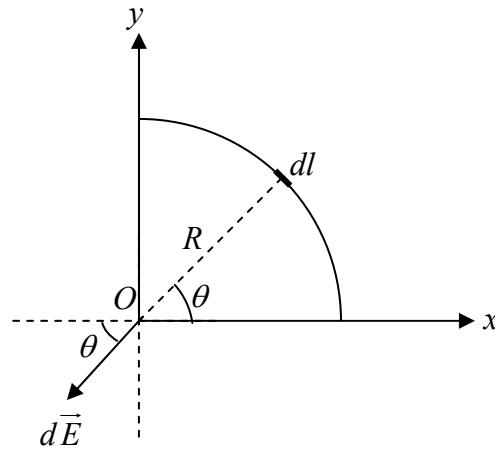
$$E_x = \int_{line} \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2} \cos \theta = \frac{\lambda}{4\pi\epsilon_0} \int_0^{\pi/2} \cos \theta \frac{R d\theta}{R^2}$$

$$\Rightarrow E_x = \frac{\lambda}{4\pi\epsilon_0 R} [\sin \theta]_0^{\pi/2} = \frac{\lambda}{4\pi\epsilon_0 R}$$

$$\text{Similarly } E_y = \int_{line} \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2} \sin \theta = \frac{\lambda}{4\pi\epsilon_0} \int_0^{\pi/2} \sin \theta \frac{R d\theta}{R^2}$$

$$\Rightarrow E_y = \frac{\lambda}{4\pi\epsilon_0 R} [-\cos \theta]_0^{\pi/2} = \frac{\lambda}{4\pi\epsilon_0 R}$$

$$\text{Thus } \vec{E} = -E_x\hat{x} - E_y\hat{y} = \frac{\lambda}{4\pi\epsilon_0 R}(-\hat{x} - \hat{y})$$



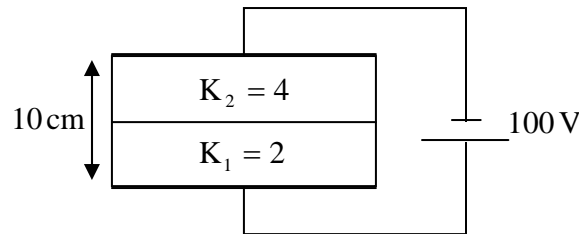
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Q17. In a parallel plate capacitor the distance between the plates is 10 cm. Two dielectric slabs of thickness 5 cm each and dielectric constants $K_1 = 2$ and $K_2 = 4$ respectively, are inserted between the plates. A potential of 100 V is applied across the capacitor as shown in the figure. The value of the net bound surface charge density at the interface of the two dielectrics is



- (a) $-\frac{2000}{3}\epsilon_0$ (b) $-\frac{1000}{3}\epsilon_0$ (c) $-250\epsilon_0$ (d) $\frac{2000}{3}\epsilon_0$

Ans.: (a)

Solution: $V = E_1 d + E_2 d = \frac{\sigma}{\epsilon_1} d + \frac{\sigma}{\epsilon_2} d = \frac{\sigma}{2\epsilon_0} d + \frac{\sigma}{4\epsilon_0} d = \frac{3\sigma}{4\epsilon_0} d$

$V = 100$ volts, $d = 5 \times 10^{-2}$ cm

$\Rightarrow \sigma = \frac{4\epsilon_0}{3d} V = \frac{4\epsilon_0}{3 \times 5 \times 10^{-2}} \times 100 = \frac{4 \times 10^4}{15} \epsilon_0$

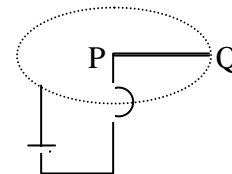
$\vec{P}_1 = \epsilon_0 \chi_e \vec{E}_1 = \epsilon_0 (K_1 - 1) \vec{E}_1 \Rightarrow \sigma_1 = \epsilon_0 \times \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{2}$

$\vec{P}_2 = \epsilon_0 \chi_e \vec{E}_2 = \epsilon_0 (K_2 - 1) \vec{E}_2 \Rightarrow \sigma_2 = 3\epsilon_0 \times \frac{\sigma}{4\epsilon_0} = \frac{3\sigma}{4}$

$\Rightarrow \sigma = \sigma_1 - \sigma_2 = \frac{\sigma}{2} - \frac{3\sigma}{4} = -\frac{\sigma}{4} = -\frac{1}{4} \times \frac{4 \times 10^4}{15} \epsilon_0 = -\frac{2000}{3} \epsilon_0$

Q18. A rigid uniform horizontal wire PQ of mass M , pivoted at P, carries a constant current I .

It rotates with a constant angular speed in a uniform vertical magnetic field B . If the current were switched off, the angular acceleration of the wire, in terms of B , M and I would be



- (a) 0 (b) $\frac{2BI}{3M}$ (c) $\frac{3BI}{2M}$ (d) $\frac{BI}{M}$

Ans.: (c)

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- Q19. A steady current in a straight conducting wire produces a surface charge on it. Let E_{out} and E_{in} be the magnitudes of the electric fields just outside and just inside the wire, respectively. Which of the following statements is true for these fields?
- (a) E_{out} is always greater than E_{in}
 (b) E_{out} is always smaller than E_{in}
 (c) E_{out} could be greater or smaller than E_{in}
 (d) E_{out} is equal to E_{in}

Ans.: (a)

- Q20. A small charged spherical shell of radius 0.01 m is at a potential of 30 V. The electrostatic energy of the shell is
- (a) 10^{-10} J (b) 5×10^{-10} J (c) 5×10^{-9} J (d) 10^{-9} J

Ans.: (b)

Solution: $V = \frac{q}{4\pi\epsilon_0 R}$ and $W = \frac{q^2}{8\pi\epsilon_0 R}$.

$$\text{Thus } W = \frac{(4\pi\epsilon_0 VR)^2}{8\pi\epsilon_0 R} = \frac{4\pi\epsilon_0 V^2 R}{2} = \frac{900 \times 10^{-2}}{9 \times 10^9 \times 2} = 0.5 \times 10^{-9} = 5 \times 10^{-10} \text{ Joules}$$

- Q21. A ring of radius R carries a linear charge density λ . It is rotating with angular speed ω . The magnetic field at its center is
- (a) $\frac{3\mu_0\lambda\omega}{2}$ (b) $\frac{\mu_0\lambda\omega}{2}$ (c) $\frac{\mu_0\lambda\omega}{\pi}$ (d) $\mu_0\lambda\omega$

Ans.: (b)

Solution: $B = \frac{\mu_0 I}{2R}$ where $I = \lambda v = \lambda R \omega$. Thus $B = \frac{\mu_0 \lambda \omega}{2}$.

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IIT-JAM-2015

Q22. The electric field of a light wave is given by $\vec{E} = E_0 \left[\hat{i} \sin(\omega t - kz) + \hat{j} \sin\left(\omega t - kz - \frac{\pi}{4}\right) \right]$.

The polarization state of the wave is

- (a) Left handed circular (b) Right handed circular
(c) Left handed elliptical (d) Right handed elliptical

Ans.: (c)

Solution: $E_x = E_0 \sin(\omega t - kz)$, $E_y = E_0 \sin\left(\omega t - kz - \frac{\pi}{4}\right)$.

Thus resultant is elliptically polarized wave.

At $z = 0$, $E_x = E_0 \sin(\omega t)$, $E_y = E_0 \sin\left(\omega t - \frac{\pi}{4}\right)$

When $\omega t = 0$, $E_x = 0$, $E_y = -\frac{E_0}{\sqrt{2}}$ and when $\omega t = \frac{\pi}{4}$, $E_x = \frac{E_0}{\sqrt{2}}$, $E_y = 0$

Q23. A charge q is at the center of two concentric spheres. The outward electric flux through the inner sphere is ϕ while that through the outer sphere is 2ϕ . The amount of charge contained in the region between the two spheres is

- (a) $2q$ (b) q (c) $-q$ (d) $-2q$

Ans.: (b)

Solution: $\phi = \frac{q}{\epsilon_0}$, $\phi' = 2\phi = \frac{q + q'}{\epsilon_0} \Rightarrow q' = q$

Q24. A positively charged particle, with a charge q , enters a region in which there is a uniform electric field \vec{E} and a uniform magnetic field \vec{B} , both directed parallel to the positive y -axis. At $t = 0$, the particle is at the origin and has a speed v_0 directed along the positive x -axis. The orbit of the particle, projected on the x - z plane, is a circle. Let T be the time taken to complete one revolution of this circle. The y -coordinate of the particle at $t = T$ is given by

- (a) $\frac{\pi^2 m E}{2qB^2}$ (b) $\frac{2\pi^2 m E}{qB^2}$ (c) $\frac{\pi^2 m E}{qB^2} + \frac{v_0 \pi m}{qB}$ (d) $\frac{2\pi m v_0}{qB}$

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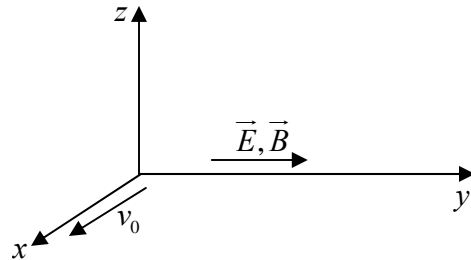
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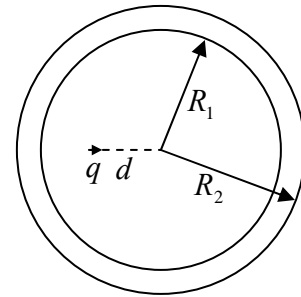
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Ans.: (b)

$$\text{Solution: } y = u_y t + \frac{1}{2} a_y t^2 \Rightarrow y = \frac{1}{2} \frac{qE}{m} \left(\frac{2\pi m}{qB} \right)^2 = \frac{2\pi^2 m E}{qB^2}$$



Q25. A hollow, conducting spherical shell of inner radius R_1 and outer radius R_2 encloses a charge q inside, which is located at a distance $d (< R_1)$ from the centre of the spheres. The potential at the centre of the shell is



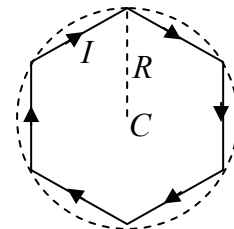
- (a) Zero
 (b) $\frac{1}{4\pi\epsilon_0} \frac{q}{d}$
 (c) $\frac{1}{4\pi\epsilon_0} \left(\frac{q}{d} - \frac{q}{R_1} \right)$
 (d) $\frac{1}{4\pi\epsilon_0} \left(\frac{q}{d} - \frac{q}{R_1} + \frac{q}{R_2} \right)$

Ans.: (d)

Solution: charge induced on inner surface is $-q$ and charge induced on outer surface is $+q$.

$$\text{Thus } V = \frac{1}{4\pi\epsilon_0} \left(\frac{q}{d} - \frac{q}{R_1} + \frac{q}{R_2} \right).$$

Q26. A conducting wire is in the shape of a regular hexagon, which is inscribed inside an imaginary circle of radius R , as shown. A current I flows through the wire. The magnitude of the magnetic field at the center of the circle is

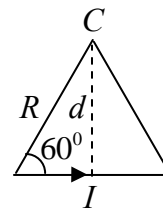


- (a) $\frac{\sqrt{3}\mu_0 I}{2\pi R}$
 (b) $\frac{\mu_0 I}{2\sqrt{3}\pi R}$
 (c) $\frac{\sqrt{3}\mu_0 I}{\pi R}$
 (d) $\frac{3\mu_0 I}{2\pi R}$

Ans.: (c)

$$\text{Solution: } d = R \cos 30^\circ = \frac{\sqrt{3}}{2} R$$

$$\therefore B = \frac{\mu_0 I}{4\pi d} (\sin \theta_2 - \sin \theta_1)$$



$$\Rightarrow B_1 = \frac{\mu_0 I}{4\pi d} 2 \sin 30^\circ = \frac{\mu_0 I}{4\pi \frac{\sqrt{3}}{2} R} 2 \sin 30^\circ = \frac{\mu_0 I}{2\sqrt{3}\pi R}$$

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$$\Rightarrow B = 6B_1 = 6 \times \frac{\mu_0 I}{2\sqrt{3}\pi R} = \frac{3\mu_0 I}{\sqrt{3}\pi R} = \frac{\sqrt{3}\mu_0 I}{\pi R}$$

SECTION-B: MSQ

Q27. For an electromagnetic wave traveling in free space, the electric field is given

by $\vec{E} = 100 \cos(10^8 t + kx) \hat{j} \frac{V}{m}$. Which of the following statements are true?

- (a) The wavelength of the wave in meter is 6π
- (b) The corresponding magnetic field is directed along the positive z direction
- (c) The Poynting vector is directed along the positive z direction
- (d) The wave is linearly polarized

Ans.: (a) and (d)

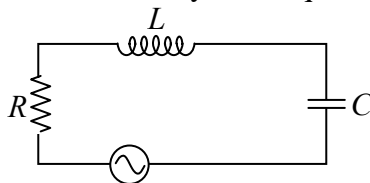
Solution: $\vec{E} = 100 \cos(10^8 t + kx) \hat{j} \text{ V/m}$

$$\omega = 10^8 \Rightarrow \frac{2\pi c}{\lambda} = 10^8 \Rightarrow \lambda = \frac{2\pi \times 3 \times 10^8}{10^8} = 6\pi. \text{ Option (a) is true}$$

$$\vec{B} \propto (\hat{k} \times \vec{E}) \propto (-\hat{x} \times \hat{y}) \propto -\hat{z}. \text{ Option (b) is wrong}$$

$$\vec{S} \propto \hat{k} \propto -\hat{x}. \text{ Option (c) is wrong. Option (d) is true.}$$

Q28. Consider the circuit, consisting of an AC function generator $V(t) = V_0 \sin 2\pi\nu t$ with $V_0 = 5V$ an inductor $L = 8.0mH$, resistor $R = 5\Omega$ and a capacitor $C = 100\mu F$. Which of the following statements are true if we vary the frequency?



- (a) The current in the circuit would be maximum at $\nu = 178Hz$
- (b) The capacitive reactance increases with frequency
- (c) At resonance, the impedance of the circuit is equal to the resistance in the circuit
- (d) At resonance, the current in the circuit is out of phase with the source voltage

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Ans.: (a) and (c)

Solution: $\nu = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2 \times 3.14 \sqrt{(8 \times 10^{-3})(100 \times 10^{-6})}} = 178 \text{ Hz}$. Option (a) is true.

$X_C = \frac{1}{\omega C} \Rightarrow X_C \downarrow \text{ as } \omega \uparrow$. Option (b) is wrong

Option (c) is true

Option (d) is wrong

Q29. A unit cube made of a dielectric material has a polarization $\vec{P} = 3\hat{i} + 4\hat{j}$ units. The edges of the cube are parallel to the Cartesian axes. Which of the following statements are true?

- (a) The cube carries a volume bound charge of magnitude 5 units
- (b) There is a charge of magnitude 3 units on both the surfaces parallel to the $y - z$ plane
- (c) There is a charge of magnitude 4 units on both the surfaces parallel to the $x - z$ plane
- (d) There is a net non-zero induced charge on the cube

Ans.: (b) and (c)

Solution: $\because \vec{P} = 3\hat{i} + 4\hat{j} \Rightarrow \rho_b = -\nabla \cdot \vec{P} = 0$. Option (a) is wrong

At $x = 0$, $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (-\hat{i}) = -3$, At $x = 1$, $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (\hat{i}) = 3$

Option (b) is true

At $y = 0$, $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (-\hat{j}) = -4$, At $y = 1$, $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (\hat{j}) = 4$

Option (c) is true.

Option (d) is wrong

Q30. The power radiated by sun is $3.8 \times 10^{26} \text{ W}$ and its radius is $7 \times 10^5 \text{ km}$. The magnitude of the Poynting vector (in $\frac{\text{W}}{\text{cm}^2}$) at the surface of the sun is.....

Ans.: 6174

Solution: $I = \frac{P}{A} = \frac{3.8 \times 10^{26}}{4\pi \times (7 \times 10^{10})^2} \text{ W/cm}^2 = 6174 \text{ W/cm}^2$

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Q31. In an experiment on charging of an initially uncharged capacitor, an RC circuit is made with the resistance $R = 10k\Omega$ and the capacitor $C = 1000\mu F$ along with a voltage source of $6V$. The magnitude of the displacement current through the capacitor (in μA), 5 seconds after the charging has started, is.....

Ans.: 364

$$\text{Solution: } I = \frac{V}{R} e^{-t/RC} = \frac{6}{10 \times 10^3} e^{-5/10 \times 10^3 \times 1000 \times 10^{-6}} = \frac{6}{10^4} e^{-5/10} = \frac{6}{\sqrt{e} \times 10^4} = \frac{6}{1.65 \times 10^4} = 364 \mu A$$

Q32. In a region of space, a time dependent magnetic field $B(t) = 0.4t$ tesla points vertically upwards. Consider a horizontal, circular loop of radius $2cm$ in this region. The magnitude of the electric field (in mV/m) induced in the loop is.....

Ans.: 4

$$\text{Solution: } \left| \vec{E} \right| \times 2\pi r = -\frac{\partial B}{\partial t} \times \pi r^2 \Rightarrow \left| \vec{E} \right| = \frac{r}{2} \frac{\partial B}{\partial t} = \frac{2 \times 10^{-2}}{2} \times 0.4 = 4 \text{ mV/m}$$

Q33. A plane electromagnetic wave of frequency $5 \times 10^{14} Hz$ and amplitude $10^3 V/m$ traveling in a homogeneous dielectric medium of dielectric constant 1.69 is incident normally at the interface with a second dielectric medium of dielectric constant 2.25. The ratio of the amplitude of the transmitted wave to that of the incident wave is.....

Ans.: 0.93

$$\text{Solution: } E_{0T} = \left(\frac{2n_1}{n_1 + n_2} \right) E_{0I} \Rightarrow \frac{E_{0T}}{E_{0I}} = \left(\frac{2\sqrt{\epsilon_{r1}}}{\sqrt{\epsilon_{r1}} + \sqrt{\epsilon_{r2}}} \right) = \left(\frac{2\sqrt{1.69}}{\sqrt{1.69} + \sqrt{2.25}} \right) = 0.93$$

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Q34. For an infinitely long wire with uniform line-charge density, λ along the z -axis, the electric field at a point $(a, b, 0)$ away from the origin is

(\hat{e}_x, \hat{e}_y and \hat{e}_z are unit vectors in Cartesian – coordinate system)

- (a) $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}(\hat{e}_x + \hat{e}_y)$ (b) $\frac{\lambda}{2\pi\epsilon_0(a^2+b^2)}(a\hat{e}_x + b\hat{e}_y)$
- (c) $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}\hat{e}_x$ (d) $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}\hat{e}_z$

Ans.: (b)

Solution: $\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} \hat{r} = \frac{\lambda}{2\pi\epsilon_0 r^2} \vec{r} = \frac{\lambda}{2\pi\epsilon_0(a^2+b^2)}(a\hat{e}_x + b\hat{e}_y) \quad \because r = \sqrt{a^2+b^2}$

Q35. A 1 W point source at origin emits light uniformly in all the directions. If the units for both the axes are measured in centimeter, then the Poynting vector at the point $(1,1,0)$ in

$\frac{W}{cm^2}$ is

- (a) $\frac{1}{8\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$ (b) $\frac{1}{16\pi}(\hat{e}_x + \hat{e}_y)$
- (c) $\frac{1}{16\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$ (d) $\frac{1}{4\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$

Ans.: (a)

Solution: $I = \langle \vec{S} \rangle = \frac{P}{A} \hat{r} = \frac{P}{4\pi r^2} \frac{\vec{r}}{r} = \frac{P}{4\pi r^3} \vec{r} = \frac{1}{4\pi \times 2\sqrt{2}}(\hat{x} + \hat{y}) = \frac{1}{8\pi\sqrt{2}}(\hat{x} + \hat{y})$

$\because r = \sqrt{1^2 + 1^2} = \sqrt{2}$

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Q36. A charged particle in a uniform magnetic field $\vec{B} = B_0 \hat{e}_z$ starts moving from the origin with velocity $\vec{v} = (3\hat{e}_x + 2\hat{e}_z) m/s$. The trajectory of the particle and the time t at which it reaches 2 meters above the xy -plane are

(\hat{e}_x, \hat{e}_y and \hat{e}_z are unit vectors in Cartesian-coordinate system)

(a) Helical path; $t = 1s$

(b) Helical path; $t = 2/3s$

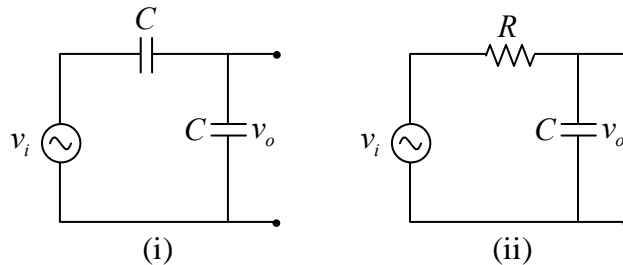
(c) Circular path; $t = 1s$

(d) Circular path; $t = 2/3s$

Ans.: (a)

Solution: $v_{\perp} = 3 m/s$ and $v_{\parallel} = 2 m/s$, thus $t = \frac{2m}{v_{\parallel}} = 1 \text{ sec}$

Q37. The phase difference (δ) between input and output voltage for the following circuits (i) and (ii)



will be

(a) 0 and 0

(b) $\pi/2$ and $0 < \delta \leq \pi/2$ respectively

(c) $\pi/2$ and $\pi/2$

(d) 0 and $0 < \delta \leq \pi/2$ respectively

Ans.: (d)

(i) $v_o = \frac{X_C}{X_C + X_C} v_i \Rightarrow \frac{v_o}{v_i} = \frac{1}{2}$, phase difference (δ) is 0.

(ii) $v_o = \frac{X_C}{R + X_C} v_i \Rightarrow \frac{v_o}{v_i} = \frac{1}{1 + R/X_C} = \frac{1}{1 + i\omega CR} = \frac{1}{\sqrt{1 + (\omega CR)^2}} e^{-i\omega CR}$

Phase difference (δ) is $0 < \delta \leq \pi/2$.

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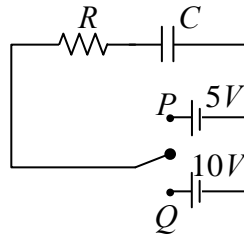
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Q38. In the following RC circuit, the capacitor was charged in two different ways.

- (i) The capacitor was first charged to $5V$ by moving the toggle switch to position P and then it was charged to $10V$ by moving the toggle switch to position Q .
- (ii) The capacitor was directly charged to $10V$, by keeping the toggle switch at position Q .

Assuming the capacitor to be ideal, which one of the following statements is correct?



- (a) The energy dissipation in cases (i) and (ii) will be equal and non-zero
- (b) The energy dissipation for case (i) will be more than that for case (ii)
- (c) The energy dissipation for case (i) will be less than that for case (ii)
- (d) The energy will not be dissipated in either case.

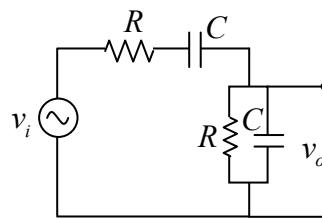
Ans.: (c)

Solution: The energy dissipation in cases (i) is $= \frac{1}{2} C(5)^2 + \frac{1}{2} C(10-5)^2 = 25C$

The energy dissipation in cases (ii) is $= \frac{1}{2} C(10)^2 = 50C$

Q39. In the following RC network, for an input signal frequency $f = \frac{1}{2\pi RC}$, the voltage gain

$\left| \frac{v_o}{v_i} \right|$ and the phase angle ϕ between v_o and v_i respectively are



- (a) $\frac{1}{2}$ and 0
- (b) $\frac{1}{3}$ and 0
- (c) $\frac{1}{2}$ and $\frac{\pi}{2}$
- (d) $\frac{1}{3}$ and $\frac{\pi}{2}$

Ans.: (b)

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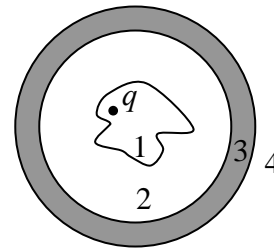
Solution: $\because f = \frac{1}{2\pi RC}$ then $X_C = \frac{1}{j2\pi fC} = -jR$

$$Z_P = \frac{RX_C}{R+X_C} = \frac{-jR^2}{R-jR} = \frac{-jR}{1-j} = \frac{-j(1+j)R}{2} \quad \text{and} \quad Z_S = R+X_C = R-jR = R(1-j)$$

$$v_o = \frac{Z_P}{Z_P+Z_S} v_i \Rightarrow \frac{v_o}{v_i} = \frac{1}{1+\frac{Z_S}{Z_P}} = \frac{1}{1+\frac{R(1-j)}{-j(1+j)R}} = \frac{1}{1-\frac{2R(1-j)}{j(1+j)R}} = \frac{j(1+j)R}{jR-R-2R(1-j)}$$

$$\Rightarrow \frac{v_o}{v_i} = \frac{j(1+j)R}{jR-R-2R(1-j)} = \frac{j(1+j)R}{3jR-3R} = \frac{(j-1)}{3(j-1)} = \frac{1}{3}$$

Q40. An arbitrarily shaped conductor encloses a charge q and is surrounded by a conducting hollow sphere as shown in the figure. Four different regions of space, 1, 2, 3 and 4 are indicated in the figure. Which one of the following statements is correct?



- (a) The electric field lines in region 2 are not affected by the position of the charge q
- (b) The surface charge density on the inner wall of the hollow sphere is uniform
- (c) The surface charge density on the outer surface of the sphere is always uniform irrespective of the position of charge q in region 1
- (d) The electric field in region 2 has a radial symmetry

Ans.: (c)

Q41. Consider a small bar magnet undergoing simple harmonic motion (SHM) along the x -axis. A coil whose plane is perpendicular to the x -axis is placed such that the magnet passes in and out of it during its motion. Which one of the following statements is correct? Neglect damping effects.

- (a) Induced e.m.f. is minimum when the center of the bar magnet crosses the coil
- (b) The frequency of the induced current in the coil is half of the frequency of the SHM
- (c) Induced e.m.f. in the coil will not change with the velocity of the magnet
- (d) The sign of the e.m.f. depends on the pole (N or S) face of the magnet which enters into the coil

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Ans.: (a)

Q42. Consider a spherical dielectric material of radius 'a' centered at origin. If the polarization vector, $\vec{P} = P_0 \hat{e}_x$, where P_0 is a constant of appropriate dimensions, then

(\hat{e}_x, \hat{e}_y , and \hat{e}_z are unit vectors in Cartesian- coordinate system)

- (a) the bound volume charge density is zero.
- (b) the bound surface charge density is zero at $(0, 0, a)$.
- (c) the electric field is zero inside the dielectric
- (d) the sign of the surface charge density changes over the surface.

Ans.: (a), (b), (d)

Solution: $\rho_b = -\vec{\nabla} \cdot \vec{P} = 0$

$$\sigma_b = \vec{P} \cdot \hat{n} = (P_0 \hat{x}) \cdot \hat{r} = P_0 \sin \theta \cos \phi = 0 \text{ at } (0, 0, a) \because \theta = 0.$$

Q43. For an electric dipole with moment $\vec{P} = p_0 \hat{e}_z$ placed at the origin, (p_0 is a constant of appropriate dimensions and \hat{e}_x, \hat{e}_y and \hat{e}_z are unit vectors in Cartesian coordinate system)

- (a) potential falls as $\frac{1}{r^2}$, where r is the distance from origin
- (b) a spherical surface centered at origin is an equipotential surface
- (c) electric flux through a spherical surface enclosing the origin is zero
- (d) radial component of \vec{E} is zero on the xy - plane.

Ans.: (a), (c), (d)

$$\text{Solution: } V_{dip}(r, \theta) = \frac{\hat{r} \cdot \vec{p}}{4\pi\epsilon_0 r^2} = \frac{p \cos \theta}{4\pi\epsilon_0 r^2}.$$

$$\vec{E}_{dip}(r, \theta) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta}).$$

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