

Electricity and MagnetismOBJECTIVE QUESTIONSIT-JAM-2005

Q1. A small loop of wire of area  $A = 0.01 \text{ m}^2$ ,  $N = 40$  turns and resistance  $R = 20 \Omega$  is initially kept in a uniform magnetic field  $B$  in such a way that the field is normal to the loop. When it is pulled out of the magnetic field, a total charge of  $Q = 2 \times 10^{-5} \text{ C}$  flows through the coil. The magnetic of the field  $B$  is

- (a)  $1 \times 10^{-3} \text{ T}$  (b)  $4 \times 10^{-3} \text{ T}$   
 (c) zero (d) unobtainable, as the data is insufficient

Ans.: (a)

Solution: Magnetic flux through the loop  $\phi = NBA$

$$\text{Induced e.m.f } \varepsilon = -\frac{d\phi}{dt} \text{ and induced current } i = -\frac{1}{R} \frac{d\phi}{dt} = \frac{dQ}{dt} \Rightarrow -\frac{1}{R} d\phi = dQ.$$

$$\text{Thus } \frac{1}{20} \times (40 \times B \times 0.01) = 2 \times 10^{-5} \Rightarrow B = 1 \times 10^{-3} \text{ T}.$$

Q2. Two point charges  $+q_1$  and  $+q_2$  are fixed with a finite distance  $d$  between them. It is desired to put a third charge  $q_3$  in between these two charges on the line joining them so that the charge  $q_3$  is in equilibrium. This is

- (a) possible only if  $q_3$  is positive  
 (b) possible only if  $q_3$  is negative  
 (c) possible irrespective of the sign of  $q_3$   
 (d) not possible at all

Ans.: (c)

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IIT-JAM-2006

Q3. Two electric dipoles  $P_1$  and  $P_2$  are placed at  $(0,0,0)$  and  $(1,0,0)$  respectively with both of them pointing in the  $+z$  direction. Without changing the orientations of the dipoles  $P_2$  is moved to  $(0,2,0)$ . The ratio of the electrostatic potential energy of the dipoles after moving to that before moving is

- (a)  $\frac{1}{16}$                       (b)  $\frac{1}{2}$                       (c)  $\frac{1}{4}$                       (d)  $\frac{1}{8}$

Ans: (d)

Solution: Electrostatic potential energy  $U \propto \frac{1}{r^3} \Rightarrow \frac{U_2}{U_1} = \frac{r_1^3}{r_2^3} = \frac{1}{8}$

Q4. A small magnetic dipole is kept at the origin in the  $x$ - $y$  plane. One wire  $L_1$  is located at  $z = -a$  in the  $x$ - $z$  plane with a current  $I$  flowing in the positive  $x$  direction. Another wire  $L_2$  is at  $z = +a$  in  $y$ - $z$  plane with the same current  $I$  as in  $L_1$ , flowing in the positive  $y$ -direction. The angle  $\phi$  made by the magnetic dipole with respect to the positive  $x$ -axis is

- (a)  $225^\circ$                       (b)  $120^\circ$                       (c)  $45^\circ$                       (d)  $270^\circ$

Ans.: (a)

Solution: Magnetic field at  $z = 0$  due to wire at  $z = -a$  is  $\vec{B} = -B\hat{y}$ .

Magnetic field at  $z = 0$  due to wire at  $z = +a$  is  $\vec{B} = -B\hat{x}$ .

Resultant magnetic field at  $z = 0$  makes an angle of  $45^\circ$  with  $-\hat{x}$  and  $225^\circ$  with  $\hat{x}$ .

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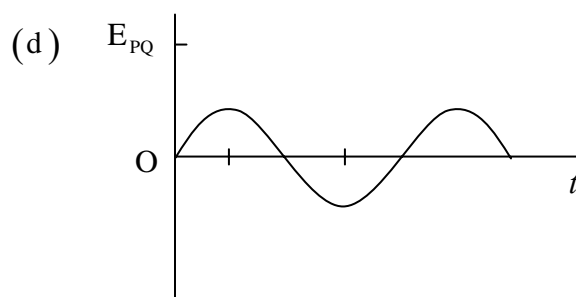
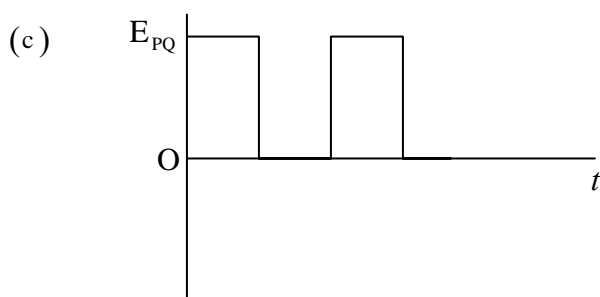
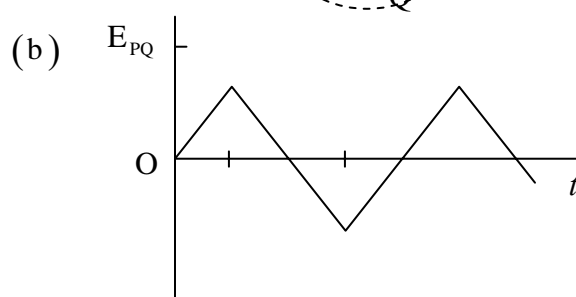
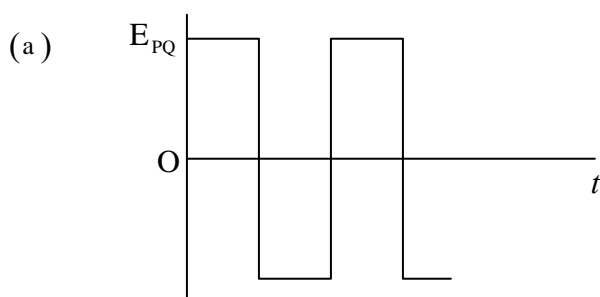
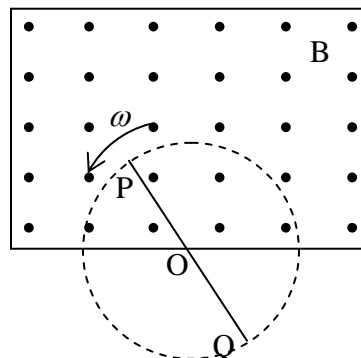
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### IIT-JAM-2007

Q5. A uniform and constant magnetic field  $B$  coming out of the plane of the paper exists in a rectangular region as shown in the figure. A conducting rod  $PQ$  is rotated about  $O$  with a uniform angular speed  $\omega$  in the plane of the paper. The emf  $E_{PQ}$  induced between  $P$  and  $Q$  is best represented by the graph



Ans.: (a)

### IIT-JAM-2008

Q6. If the electrostatic potential at a point  $(x, y)$  is given by  $V = (2x + 4y)$  volts, the electrostatic energy density at that point (in  $J/m^3$ ) is

- (a)  $5\epsilon_0$                       (b)  $10\epsilon_0$                       (c)  $20\epsilon_0$                       (d)  $\frac{1}{2}\epsilon_0(2x + 4y)^2$

Ans.: (a)

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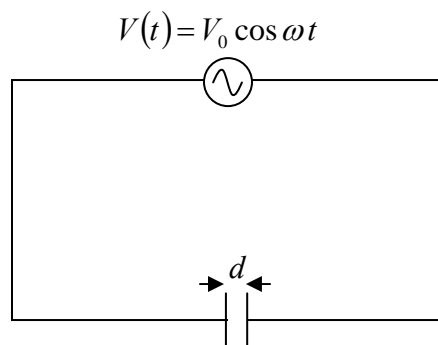
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Solution:  $\vec{E} = -\vec{\nabla}V = -2\hat{x} - 4\hat{y} \Rightarrow |\vec{E}| = 20 \text{ V/m}$

$$\text{Electrostatic energy density} = \frac{1}{2} \epsilon_0 |\vec{E}|^2 = \frac{1}{2} \epsilon_0 \times 20 = 10 \epsilon_0 \text{ J/m}^3$$

### IIT-JAM-2009

Q7. An oscillating voltage  $V(t) = V_0 \cos \omega t$  is applied across a parallel plate capacitor having a plate separation  $d$ . The displacement current density through the capacitor is



(a)  $\frac{\epsilon_0 \omega V_0 \cos \omega t}{d}$

(b)  $\frac{\epsilon_0 \mu_0 \omega V_0 \cos \omega t}{d}$

(c)  $-\frac{\epsilon_0 \mu_0 \omega V_0 \cos \omega t}{d}$

(d)  $-\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Ans.: (d)

Solution: Displacement current density  $J_d = \epsilon_0 \frac{\partial E}{\partial t} = \frac{\epsilon_0}{d} \frac{\partial V(t)}{\partial t} = -\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Q8. An electric field  $\vec{E}(\vec{r}) = (\alpha \hat{r} + \beta \sin \theta \cos \phi \hat{\phi})$  exists in space. What will be the total charge enclosed in a sphere of unit radius centered at the origin?

(a)  $4\pi\epsilon_0\alpha$

(b)  $4\pi\epsilon_0(\alpha + \beta)$

(c)  $4\pi\epsilon_0(\alpha - \beta)$

(d)  $4\pi\epsilon_0\beta$

Ans.: (a)

Solution:  $Q_{enc} = \epsilon_0 \oint \vec{E} \cdot d\vec{a} = \epsilon_0 \int (\alpha \hat{r} + \beta \sin \theta \cos \phi \hat{\phi}) \cdot (r^2 \sin \theta d\theta d\phi \hat{r}) = 4\pi\alpha\epsilon_0$

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## IIT-JAM-2010

Q9. The magnetic field associated with the electric field vector  $\vec{E} = E_0 \sin(kz - \omega t)\hat{j}$  is given by

(a)  $\vec{B} = -\frac{E_0}{c} \sin(kz - \omega t)\hat{i}$

(b)  $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{i}$

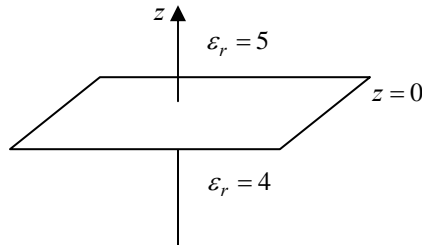
(c)  $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{j}$

(d)  $\vec{B} = \frac{E_0}{c} \sin(kz - \omega t)\hat{k}$

Ans.: (a)

Solution:  $\vec{B} = \frac{\vec{k} \times \vec{E}}{\omega} = \frac{k\hat{z} \times E_0 \sin(kz - \omega t)\hat{j}}{\omega} = -\frac{kE_0}{\omega} \sin(kz - \omega t)\hat{x} = -\frac{E_0}{c} \sin(kz - \omega t)\hat{x}$

Q10. Assume that  $z = 0$  plane is the interface between two linear and homogenous dielectrics (see figure). The relative permittivities are  $\epsilon_r = 5$  for  $z > 0$  and  $\epsilon_r = 4$  for  $z < 0$ . The electric field in the region  $z > 0$  is  $\vec{E}_1 = (3\hat{i} - 5\hat{j} + 4\hat{k})kV/m$ . If there are no free charges on the interface, the electric field in the region  $z < 0$  is given by



(a)  $\vec{E}_2 = \left(\frac{3}{4}\hat{i} - \frac{5}{4}\hat{j} + \hat{k}\right)kV/m$

(b)  $\vec{E}_2 = (3\hat{i} - 5\hat{j} + \hat{k})kV/m$

(c)  $\vec{E}_2 = (3\hat{i} - 5\hat{j} - 5\hat{k})kV/m$

(d)  $\vec{E}_2 = (3\hat{i} - 5\hat{j} + 5\hat{k})kV/m$

Ans.: (d)

Solution:  $\because E_1^\perp = E_2^\perp \Rightarrow E_2^\perp = 3\hat{i} - 5\hat{j}$

and  $\sigma_f = 0 \Rightarrow D_1^\perp = D_2^\perp \Rightarrow E_2^\perp = \frac{\epsilon_1}{\epsilon_2} E_1^\perp = \frac{5}{4}(3\hat{i} - 5\hat{j}) = 3.75\hat{i} - 6.25\hat{j}$

$\Rightarrow \vec{E}_2 = (3\hat{i} - 5\hat{j} + 5\hat{k})kV/m$

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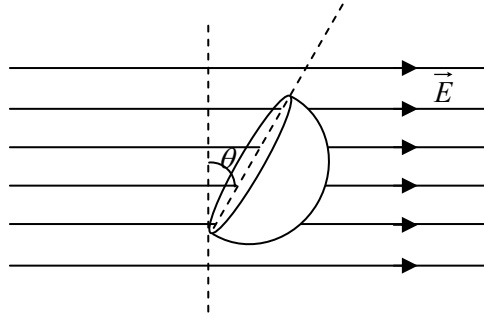
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Q11. A closed Gaussian surface consisting of a hemisphere and a circular disc of radius  $R$ , is placed in a uniform electric field  $\vec{E}$ , as shown in the figure. The circular disc makes an angle  $\theta = 30^\circ$  with the vertical. The flux of the electric field vector coming out of the curved surface of the hemisphere is

- (a)  $\frac{1}{2} \pi R^2 E$   
 (b)  $\frac{\sqrt{3}}{2} \pi R^2 E$   
 (c)  $\pi R^2 E$   
 (d)  $2\pi R^2 E$



Ans.: (b)

Solution:  $\vec{E} = E \cos 30 \hat{z} + E \sin 30 \hat{x} = \frac{\sqrt{3}}{2} E \hat{z} + \frac{1}{2} E \hat{x}$

$$\phi_E = \int_S \vec{E} \cdot d\vec{a} = \int \int \left( \frac{\sqrt{3}}{2} E \hat{z} + \frac{1}{2} E \hat{x} \right) \cdot (R^2 \sin \theta d\theta d\phi \hat{r})$$

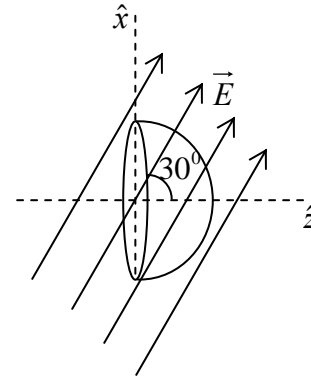
$$\phi_E = R^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} \left( \frac{\sqrt{3}}{2} E \cos \theta + \frac{1}{2} E \sin \theta \cos \phi \right) (\sin \theta d\theta d\phi)$$

$$\phi_E = \frac{\sqrt{3}}{2} ER^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} (\cos \theta \sin \theta) d\theta d\phi + \frac{1}{2} ER^2 \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} (\sin^2 \theta \cos \phi) d\theta d\phi$$

$$\phi_E = \frac{\sqrt{3}}{2} ER^2 \times 2\pi \times \frac{1}{2} + 0 = \frac{\sqrt{3}}{2} \pi R^2 E$$

OR

$$\phi_E = \int_S \vec{E} \cdot d\vec{a} = E \cos 30^\circ \times \pi R^2 = \frac{\sqrt{3}}{2} \pi R^2 E$$



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### IIT-JAM-2011

Q12. Equipotential surface corresponding to a particular charge distribution are given by  $4x^2 + (y-2)^2 + z^2 = V_i$  where the values of  $V_i$  are constants. The electric field  $\vec{E}$  at the origin is

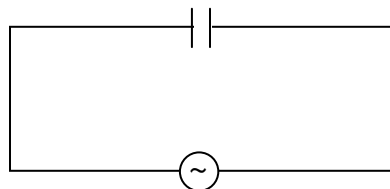
- (a)  $\vec{E} = 0$                       (b)  $\vec{E} = 2\hat{x}$                       (c)  $\vec{E} = 4\hat{y}$                       (d)  $\vec{E} = -4\hat{y}$

Ans.: (d)

Solution:  $\vec{E} = -\nabla V = 8x\hat{x} + 2(y-2)\hat{y} + 2z\hat{z} \Rightarrow \vec{E}(0,0) = -4\hat{y}$

### IIT-JAM-2012

Q13. A parallel plate air-gap capacitor is made up of two plates of area  $10 \text{ cm}^2$  each kept at a distance of  $0.88 \text{ mm}$ . A sine wave of amplitude  $10 \text{ V}$  and frequency  $50 \text{ Hz}$  is applied across the capacitor as shown in the figure. The amplitude of the displacement current density (in  $\text{mA/m}^2$ ) between the plates will be closest to



- (a) 0.03                      (b) 0.30                      (c) 3.00                      (d) 30.00

Ans.: (a)

Solution: Displacement current density  $J_d = \epsilon_0 \frac{\partial E}{\partial t} = \frac{\epsilon_0}{d} \frac{\partial V(t)}{\partial t} = -\frac{\epsilon_0 \omega V_0 \sin \omega t}{d}$

Amplitude of the displacement current density (in  $\text{mA/m}^2$ )  $J_{0d} = \frac{\epsilon_0 \omega V_0}{d} = \frac{2\pi \epsilon_0 f V_0}{d}$

$$\Rightarrow J_{0d} = 4\pi \epsilon_0 \frac{f V_0}{2d} = \frac{1}{9 \times 10^9} \frac{50 \times 10}{2 \times 88 \times 10^{-5}} = 0.03 \text{ mA/m}^2$$

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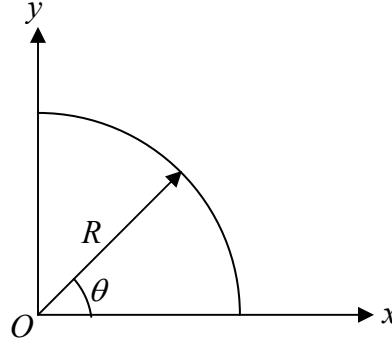
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Q14. A segment of a circular wire of radius  $R$ , extending from  $\theta = 0$  to  $\pi/2$ , carries a constant linear charge density  $\lambda$ . The electric field at origin  $O$  is

- (a)  $\frac{\lambda}{4\pi\epsilon_0 R}(-\hat{x} - \hat{y})$   
 (b)  $\frac{\lambda}{4\pi\epsilon_0 R}\left(-\frac{1}{\sqrt{2}}\hat{x} - \frac{1}{\sqrt{2}}\hat{y}\right)$   
 (c)  $\frac{\lambda}{4\pi\epsilon_0 R}\left(-\frac{1}{2}\hat{x} - \frac{1}{2}\hat{y}\right)$   
 (d) 0



Ans.: (a)

Solution:  $\vec{E} = -E_x\hat{x} - E_y\hat{y}$

where  $E_x = \int_{line} dE \cos \theta$ ,  $E_y = \int_{line} dE \sin \theta$ .

and  $dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2}$ .

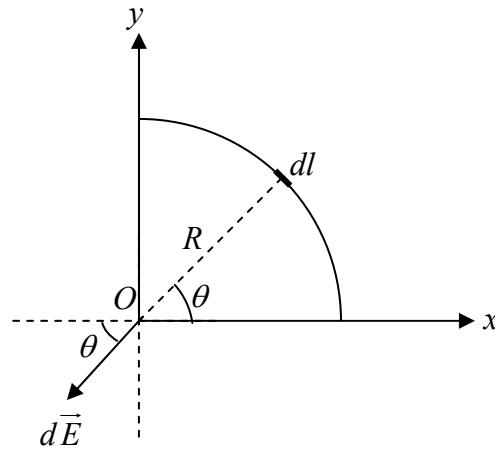
$$E_x = \int_{line} \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2} \cos \theta = \frac{\lambda}{4\pi\epsilon_0} \int_0^{\pi/2} \cos \theta \frac{R d\theta}{R^2}$$

$$\Rightarrow E_x = \frac{\lambda}{4\pi\epsilon_0 R} [\sin \theta]_0^{\pi/2} = \frac{\lambda}{4\pi\epsilon_0 R}$$

$$\text{Similarly } E_y = \int_{line} \frac{1}{4\pi\epsilon_0} \frac{\lambda dl}{R^2} \sin \theta = \frac{\lambda}{4\pi\epsilon_0} \int_0^{\pi/2} \sin \theta \frac{R d\theta}{R^2}$$

$$\Rightarrow E_y = \frac{\lambda}{4\pi\epsilon_0 R} [-\cos \theta]_0^{\pi/2} = \frac{\lambda}{4\pi\epsilon_0 R}$$

$$\text{Thus } \vec{E} = -E_x\hat{x} - E_y\hat{y} = \frac{\lambda}{4\pi\epsilon_0 R}(-\hat{x} - \hat{y})$$



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### IIT-JAM-2014

Q15. A particle of mass  $m$  carrying charge  $q$  is moving in a circle in a magnetic field  $B$ . According to Bohr's model, the energy of the particle in the  $n^{\text{th}}$  level is

- (a)  $\frac{1}{n^2} \left( \frac{hqB}{\pi m} \right)$       (b)  $n \left( \frac{hqB}{\pi m} \right)$       (c)  $n \left( \frac{hqB}{2\pi m} \right)$       (d)  $n \left( \frac{hqB}{4\pi m} \right)$

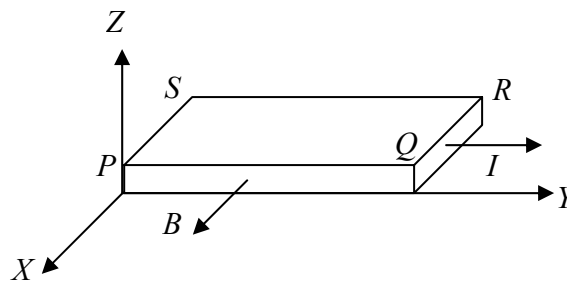
Ans.: (d)

Solution:  $E_n = \frac{q^2 B^2 r_n^2}{2m}$        $\because mv_n r_n = n\hbar$  and  $r_n = \frac{mv_n}{qB} \Rightarrow r_n = \frac{m}{qB} \frac{n\hbar}{mr_n} \Rightarrow r_n^2 = \frac{n\hbar}{qB}$

$$\Rightarrow E_n = \frac{q^2 B^2 r_n^2}{2m} = \frac{q^2 B^2}{2m} \times \frac{n\hbar}{qB} = n \left( \frac{qB\hbar}{4\pi m} \right)$$

Q16. A conducting slab of copper PQRS is kept on the  $xy$  plane in a uniform magnetic field along  $x$ -axis as indicated in the figure.

A steady current  $I$  flows through the cross section of the slab along the  $y$ -axis. The direction of the electric field inside the slab, arising due to the applied magnetic field is along the



- (a) negative Y direction      (b) positive Y direction  
(c) negative Z direction      (d) positive Z direction

Ans.: (c)

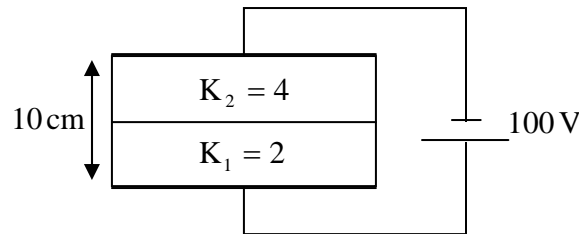
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Q17. In a parallel plate capacitor the distance between the plates is 10 cm. Two dielectric slabs of thickness 5 cm each and dielectric constants  $K_1 = 2$  and  $K_2 = 4$  respectively, are inserted between the plates. A potential of 100 V is applied across the capacitor as shown in the figure. The value of the net bound surface charge density at the interface of the two dielectrics is



- (a)  $-\frac{2000}{3}\epsilon_0$       (b)  $-\frac{1000}{3}\epsilon_0$       (c)  $-250\epsilon_0$       (d)  $\frac{2000}{3}\epsilon_0$

Ans.: (a)

Solution:  $V = E_1 d + E_2 d = \frac{\sigma}{\epsilon_1} d + \frac{\sigma}{\epsilon_2} d = \frac{\sigma}{2\epsilon_0} d + \frac{\sigma}{4\epsilon_0} d = \frac{3\sigma}{4\epsilon_0} d$

$V = 100 \text{ volts, } d = 5 \times 10^{-2} \text{ cm}$

$\Rightarrow \sigma = \frac{4\epsilon_0}{3d} V = \frac{4\epsilon_0}{3 \times 5 \times 10^{-2}} \times 100 = \frac{4 \times 10^4}{15} \epsilon_0$

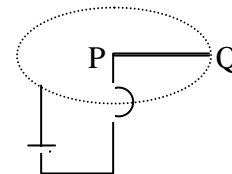
$\vec{P}_1 = \epsilon_0 \chi_e \vec{E}_1 = \epsilon_0 (K_1 - 1) \vec{E}_1 \Rightarrow \sigma_1 = \epsilon_0 \times \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{2}$

$\vec{P}_2 = \epsilon_0 \chi_e \vec{E}_2 = \epsilon_0 (K_2 - 1) \vec{E}_1 \Rightarrow \sigma_2 = 3\epsilon_0 \times \frac{\sigma}{4\epsilon_0} = \frac{3\sigma}{4}$

$\Rightarrow \sigma = \sigma_1 - \sigma_2 = \frac{\sigma}{2} - \frac{3\sigma}{4} = -\frac{\sigma}{4} = -\frac{1}{4} \times \frac{4 \times 10^4}{15} \epsilon_0 = -\frac{2000}{3} \epsilon_0$

Q18. A rigid uniform horizontal wire PQ of mass  $M$ , pivoted at P, carries a constant current  $I$ .

It rotates with a constant angular speed in a uniform vertical magnetic field  $B$ . If the current were switched off, the angular acceleration of the wire, in terms of  $B$ ,  $M$  and  $I$  would be



- (a) 0      (b)  $\frac{2BI}{3M}$       (c)  $\frac{3BI}{2M}$       (d)  $\frac{BI}{M}$

Ans.: (c)

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- Q19. A steady current in a straight conducting wire produces a surface charge on it. Let  $E_{out}$  and  $E_{in}$  be the magnitudes of the electric fields just outside and just inside the wire, respectively. Which of the following statements is true for these fields?
- (a)  $E_{out}$  is always greater than  $E_{in}$   
 (b)  $E_{out}$  is always smaller than  $E_{in}$   
 (c)  $E_{out}$  could be greater or smaller than  $E_{in}$   
 (d)  $E_{out}$  is equal to  $E_{in}$

Ans.: (a)

- Q20. A small charged spherical shell of radius 0.01 m is at a potential of 30 V. The electrostatic energy of the shell is
- (a)  $10^{-10}$  J                      (b)  $5 \times 10^{-10}$  J                      (c)  $5 \times 10^{-9}$  J                      (d)  $10^{-9}$  J

Ans.: (b)

Solution:  $V = \frac{q}{4\pi\epsilon_0 R}$  and  $W = \frac{q^2}{8\pi\epsilon_0 R}$ .

$$\text{Thus } W = \frac{(4\pi\epsilon_0 VR)^2}{8\pi\epsilon_0 R} = \frac{4\pi\epsilon_0 V^2 R}{2} = \frac{900 \times 10^{-2}}{9 \times 10^9 \times 2} = 0.5 \times 10^{-9} = 5 \times 10^{-10} \text{ Joules}$$

- Q21. A ring of radius  $R$  carries a linear charge density  $\lambda$ . It is rotating with angular speed  $\omega$ . The magnetic field at its center is
- (a)  $\frac{3\mu_0\lambda\omega}{2}$                       (b)  $\frac{\mu_0\lambda\omega}{2}$                       (c)  $\frac{\mu_0\lambda\omega}{\pi}$                       (d)  $\mu_0\lambda\omega$

Ans.: (b)

Solution:  $B = \frac{\mu_0 I}{2R}$  where  $I = \lambda v = \lambda R \omega$ . Thus  $B = \frac{\mu_0 \lambda \omega}{2}$ .

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Q22. The electric field of a light wave is given by  $\vec{E} = E_0 \left[ \hat{i} \sin(\omega t - kz) + \hat{j} \sin\left(\omega t - kz - \frac{\pi}{4}\right) \right]$ .

The polarization state of the wave is

- (a) Left handed circular (b) Right handed circular  
(c) Left handed elliptical (d) Right handed elliptical

Ans.: (c)

Solution:  $E_x = E_0 \sin(\omega t - kz)$ ,  $E_y = E_0 \sin\left(\omega t - kz - \frac{\pi}{4}\right)$ .

Thus resultant is elliptically polarized wave.

At  $z = 0$ ,  $E_x = E_0 \sin(\omega t)$ ,  $E_y = E_0 \sin\left(\omega t - \frac{\pi}{4}\right)$

When  $\omega t = 0$ ,  $E_x = 0$ ,  $E_y = -\frac{E_0}{\sqrt{2}}$  and when  $\omega t = \frac{\pi}{4}$ ,  $E_x = \frac{E_0}{\sqrt{2}}$ ,  $E_y = 0$

Q23. A charge  $q$  is at the center of two concentric spheres. The outward electric flux through the inner sphere is  $\phi$  while that through the outer sphere is  $2\phi$ . The amount of charge contained in the region between the two spheres is

- (a)  $2q$  (b)  $q$  (c)  $-q$  (d)  $-2q$

Ans.: (b)

Solution:  $\phi = \frac{q}{\epsilon_0}$ ,  $\phi' = 2\phi = \frac{q + q'}{\epsilon_0} \Rightarrow q' = q$

Q24. A positively charged particle, with a charge  $q$ , enters a region in which there is a uniform electric field  $\vec{E}$  and a uniform magnetic field  $\vec{B}$ , both directed parallel to the positive  $y$ -axis. At  $t = 0$ , the particle is at the origin and has a speed  $v_0$  directed along the positive  $x$ -axis. The orbit of the particle, projected on the  $x$ - $z$  plane, is a circle. Let  $T$  be the time taken to complete one revolution of this circle. The  $y$ -coordinate of the particle at  $t = T$  is given by

- (a)  $\frac{\pi^2 m E}{2qB^2}$  (b)  $\frac{2\pi^2 m E}{qB^2}$  (c)  $\frac{\pi^2 m E}{qB^2} + \frac{v_0 \pi m}{qB}$  (d)  $\frac{2\pi m v_0}{qB}$

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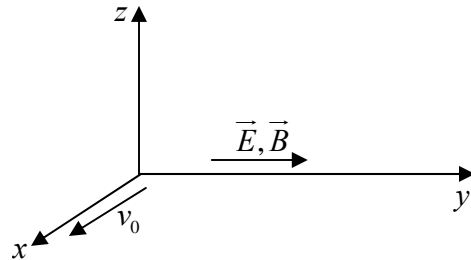
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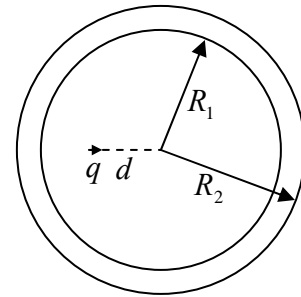
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Ans.: (b)

$$\text{Solution: } y = u_y t + \frac{1}{2} a_y t^2 \Rightarrow y = \frac{1}{2} \frac{qE}{m} \left( \frac{2\pi m}{qB} \right)^2 = \frac{2\pi^2 m E}{qB^2}$$



Q25. A hollow, conducting spherical shell of inner radius  $R_1$  and outer radius  $R_2$  encloses a charge  $q$  inside, which is located at a distance  $d (< R_1)$  from the centre of the spheres. The potential at the centre of the shell is



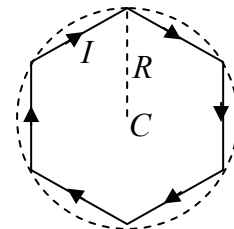
- (a) Zero  
 (b)  $\frac{1}{4\pi\epsilon_0} \frac{q}{d}$   
 (c)  $\frac{1}{4\pi\epsilon_0} \left( \frac{q}{d} - \frac{q}{R_1} \right)$   
 (d)  $\frac{1}{4\pi\epsilon_0} \left( \frac{q}{d} - \frac{q}{R_1} + \frac{q}{R_2} \right)$

Ans.: (d)

Solution: charge induced on inner surface is  $-q$  and charge induced on outer surface is  $+q$ .

$$\text{Thus } V = \frac{1}{4\pi\epsilon_0} \left( \frac{q}{d} - \frac{q}{R_1} + \frac{q}{R_2} \right).$$

Q26. A conducting wire is in the shape of a regular hexagon, which is inscribed inside an imaginary circle of radius  $R$ , as shown. A current  $I$  flows through the wire. The magnitude of the magnetic field at the center of the circle is

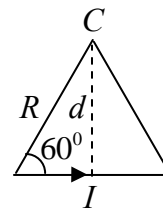


- (a)  $\frac{\sqrt{3}\mu_0 I}{2\pi R}$   
 (b)  $\frac{\mu_0 I}{2\sqrt{3}\pi R}$   
 (c)  $\frac{\sqrt{3}\mu_0 I}{\pi R}$   
 (d)  $\frac{3\mu_0 I}{2\pi R}$

Ans.: (c)

$$\text{Solution: } d = R \cos 30^\circ = \frac{\sqrt{3}}{2} R$$

$$\therefore B = \frac{\mu_0 I}{4\pi d} (\sin \theta_2 - \sin \theta_1)$$



$$\Rightarrow B_1 = \frac{\mu_0 I}{4\pi d} 2 \sin 30^\circ = \frac{\mu_0 I}{4\pi \frac{\sqrt{3}}{2} R} 2 \sin 30^\circ = \frac{\mu_0 I}{2\sqrt{3}\pi R}$$

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$$\Rightarrow B = 6B_1 = 6 \times \frac{\mu_0 I}{2\sqrt{3}\pi R} = \frac{3\mu_0 I}{\sqrt{3}\pi R} = \frac{\sqrt{3}\mu_0 I}{\pi R}$$

## SECTION-B: MSQ

Q27. For an electromagnetic wave traveling in free space, the electric field is given

by  $\vec{E} = 100 \cos(10^8 t + kx) \hat{j} \frac{V}{m}$ . Which of the following statements are true?

- (a) The wavelength of the wave in meter is  $6\pi$
- (b) The corresponding magnetic field is directed along the positive  $z$  direction
- (c) The Poynting vector is directed along the positive  $z$  direction
- (d) The wave is linearly polarized

Ans.: (a) and (d)

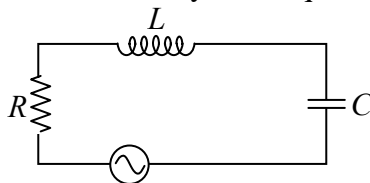
Solution:  $\vec{E} = 100 \cos(10^8 t + kx) \hat{j} \text{ V/m}$

$$\omega = 10^8 \Rightarrow \frac{2\pi c}{\lambda} = 10^8 \Rightarrow \lambda = \frac{2\pi \times 3 \times 10^8}{10^8} = 6\pi. \text{ Option (a) is true}$$

$$\vec{B} \propto (\hat{k} \times \vec{E}) \propto (-\hat{x} \times \hat{y}) \propto -\hat{z}. \text{ Option (b) is wrong}$$

$$\vec{S} \propto \hat{k} \propto -\hat{x}. \text{ Option (c) is wrong. Option (d) is true.}$$

Q28. Consider the circuit, consisting of an AC function generator  $V(t) = V_0 \sin 2\pi\nu t$  with  $V_0 = 5V$  an inductor  $L = 8.0mH$ , resistor  $R = 5\Omega$  and a capacitor  $C = 100\mu F$ . Which of the following statements are true if we vary the frequency?



- (a) The current in the circuit would be maximum at  $\nu = 178Hz$
- (b) The capacitive reactance increases with frequency
- (c) At resonance, the impedance of the circuit is equal to the resistance in the circuit
- (d) At resonance, the current in the circuit is out of phase with the source voltage

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Ans.: (a) and (c)

Solution:  $\nu = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2 \times 3.14 \sqrt{(8 \times 10^{-3})(100 \times 10^{-6})}} = 178 \text{ Hz}$ . Option (a) is true.

$X_C = \frac{1}{\omega C} \Rightarrow X_C \downarrow \text{ as } \omega \uparrow$ . Option (b) is wrong

Option (c) is true

Option (d) is wrong

Q29. A unit cube made of a dielectric material has a polarization  $\vec{P} = 3\hat{i} + 4\hat{j}$  units. The edges of the cube are parallel to the Cartesian axes. Which of the following statements are true?

(a) The cube carries a volume bound charge of magnitude 5 units

(b) There is a charge of magnitude 3 units on both the surfaces parallel to the  $y - z$  plane

(c) There is a charge of magnitude 4 units on both the surfaces parallel to the  $x - z$  plane

(d) There is a net non-zero induced charge on the cube

Ans.: (b) and (c)

Solution:  $\because \vec{P} = 3\hat{i} + 4\hat{j} \Rightarrow \rho_b = -\nabla \cdot \vec{P} = 0$ . Option (a) is wrong

At  $x = 0$ ,  $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (-\hat{i}) = -3$ , At  $x = 1$ ,  $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (\hat{i}) = 3$

Option (b) is true

At  $y = 0$ ,  $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (-\hat{j}) = -4$ , At  $y = 1$ ,  $\sigma_b = \vec{P} \cdot \hat{n} = (3\hat{i} + 4\hat{j}) \cdot (\hat{j}) = 4$

Option (c) is true.

Option (d) is wrong

Q30. The power radiated by sun is  $3.8 \times 10^{26} \text{ W}$  and its radius is  $7 \times 10^5 \text{ km}$ . The magnitude of the Poynting vector (in  $\frac{\text{W}}{\text{cm}^2}$ ) at the surface of the sun is.....

Ans.: 6174

Solution:  $I = \frac{P}{A} = \frac{3.8 \times 10^{26}}{4\pi \times (7 \times 10^{10})^2} \text{ W/cm}^2 = 6174 \text{ W/cm}^2$

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Q31. In an experiment on charging of an initially uncharged capacitor, an RC circuit is made with the resistance  $R = 10k\Omega$  and the capacitor  $C = 1000\mu F$  along with a voltage source of  $6V$ . The magnitude of the displacement current through the capacitor (in  $\mu A$ ), 5 seconds after the charging has started, is.....

Ans.: 364

$$\text{Solution: } I = \frac{V}{R} e^{-t/RC} = \frac{6}{10 \times 10^3} e^{-5/10 \times 10^3 \times 1000 \times 10^{-6}} = \frac{6}{10^4} e^{-5/10} = \frac{6}{\sqrt{e} \times 10^4} = \frac{6}{1.65 \times 10^4} = 364 \mu A$$

Q32. In a region of space, a time dependent magnetic field  $B(t) = 0.4t$  tesla points vertically upwards. Consider a horizontal, circular loop of radius  $2cm$  in this region. The magnitude of the electric field (in  $mV/m$ ) induced in the loop is.....

Ans.: 4

$$\text{Solution: } \left| \vec{E} \right| \times 2\pi r = -\frac{\partial B}{\partial t} \times \pi r^2 \Rightarrow \left| \vec{E} \right| = \frac{r}{2} \frac{\partial B}{\partial t} = \frac{2 \times 10^{-2}}{2} \times 0.4 = 4 \text{ mV/m}$$

Q33. A plane electromagnetic wave of frequency  $5 \times 10^{14} Hz$  and amplitude  $10^3 V/m$  traveling in a homogeneous dielectric medium of dielectric constant 1.69 is incident normally at the interface with a second dielectric medium of dielectric constant 2.25. The ratio of the amplitude of the transmitted wave to that of the incident wave is.....

Ans.: 0.93

$$\text{Solution: } E_{0T} = \left( \frac{2n_1}{n_1 + n_2} \right) E_{0I} \Rightarrow \frac{E_{0T}}{E_{0I}} = \left( \frac{2\sqrt{\epsilon_{r1}}}{\sqrt{\epsilon_{r1}} + \sqrt{\epsilon_{r2}}} \right) = \left( \frac{2\sqrt{1.69}}{\sqrt{1.69} + \sqrt{2.25}} \right) = 0.93$$

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Q34. For an infinitely long wire with uniform line-charge density,  $\lambda$  along the  $z$ -axis, the electric field at a point  $(a, b, 0)$  away from the origin is

( $\hat{e}_x, \hat{e}_y$  and  $\hat{e}_z$  are unit vectors in Cartesian – coordinate system)

- (a)  $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}(\hat{e}_x + \hat{e}_y)$                       (b)  $\frac{\lambda}{2\pi\epsilon_0(a^2+b^2)}(a\hat{e}_x + b\hat{e}_y)$
- (c)  $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}\hat{e}_x$                                       (d)  $\frac{\lambda}{2\pi\epsilon_0\sqrt{a^2+b^2}}\hat{e}_z$

Ans.: (b)

Solution:  $\vec{E} = \frac{\lambda}{2\pi\epsilon_0 r} \hat{r} = \frac{\lambda}{2\pi\epsilon_0 r^2} \vec{r} = \frac{\lambda}{2\pi\epsilon_0(a^2+b^2)}(a\hat{e}_x + b\hat{e}_y)$                        $\because r = \sqrt{a^2+b^2}$

Q35. A  $1\text{ W}$  point source at origin emits light uniformly in all the directions. If the units for both the axes are measured in centimeter, then the Poynting vector at the point  $(1,1,0)$  in

$\frac{W}{cm^2}$  is

- (a)  $\frac{1}{8\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$                                       (b)  $\frac{1}{16\pi}(\hat{e}_x + \hat{e}_y)$
- (c)  $\frac{1}{16\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$                                       (d)  $\frac{1}{4\pi\sqrt{2}}(\hat{e}_x + \hat{e}_y)$

Ans.: (a)

Solution:  $I = \langle \vec{S} \rangle = \frac{P}{A} \hat{r} = \frac{P}{4\pi r^2} \frac{\vec{r}}{r} = \frac{P}{4\pi r^3} \vec{r} = \frac{1}{4\pi \times 2\sqrt{2}}(\hat{x} + \hat{y}) = \frac{1}{8\pi\sqrt{2}}(\hat{x} + \hat{y})$

$\because r = \sqrt{1^2 + 1^2} = \sqrt{2}$

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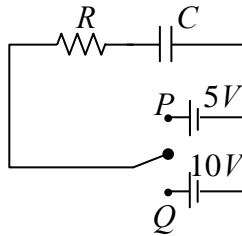
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Q38. In the following  $RC$  circuit, the capacitor was charged in two different ways.

- (i) The capacitor was first charged to  $5V$  by moving the toggle switch to position  $P$  and then it was charged to  $10V$  by moving the toggle switch to position  $Q$ .
- (ii) The capacitor was directly charged to  $10V$ , by keeping the toggle switch at position  $Q$ .

Assuming the capacitor to be ideal, which one of the following statements is correct?



- (a) The energy dissipation in cases (i) and (ii) will be equal and non-zero
- (b) The energy dissipation for case (i) will be more than that for case (ii)
- (c) The energy dissipation for case (i) will be less than that for case (ii)
- (d) The energy will not be dissipated in either case.

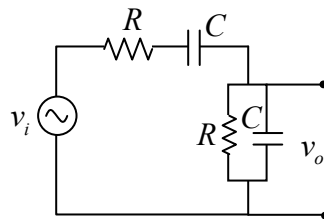
Ans.: (c)

Solution: The energy dissipation in cases (i) is  $= \frac{1}{2} C(5)^2 + \frac{1}{2} C(10-5)^2 = 25C$

The energy dissipation in cases (ii) is  $= \frac{1}{2} C(10)^2 = 50C$

Q39. In the following  $RC$  network, for an input signal frequency  $f = \frac{1}{2\pi RC}$ , the voltage gain

$\left| \frac{v_o}{v_i} \right|$  and the phase angle  $\phi$  between  $v_o$  and  $v_i$  respectively are



- (a)  $\frac{1}{2}$  and  $0$
- (b)  $\frac{1}{3}$  and  $0$
- (c)  $\frac{1}{2}$  and  $\frac{\pi}{2}$
- (d)  $\frac{1}{3}$  and  $\frac{\pi}{2}$

Ans.: (b)

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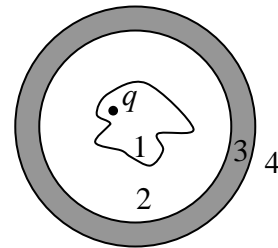
Solution:  $\because f = \frac{1}{2\pi RC}$  then  $X_C = \frac{1}{j2\pi fC} = -jR$

$$Z_P = \frac{RX_C}{R+X_C} = \frac{-jR^2}{R-jR} = \frac{-jR}{1-j} = \frac{-j(1+j)R}{2} \quad \text{and} \quad Z_S = R+X_C = R-jR = R(1-j)$$

$$v_o = \frac{Z_P}{Z_P+Z_S} v_i \Rightarrow \frac{v_o}{v_i} = \frac{1}{1+\frac{Z_S}{Z_P}} = \frac{1}{1+\frac{R(1-j)}{-j(1+j)R}} = \frac{1}{1-\frac{2R(1-j)}{j(1+j)R}} = \frac{j(1+j)R}{jR-R-2R(1-j)}$$

$$\Rightarrow \frac{v_o}{v_i} = \frac{j(1+j)R}{jR-R-2R(1-j)} = \frac{j(1+j)R}{3jR-3R} = \frac{(j-1)}{3(j-1)} = \frac{1}{3}$$

Q40. An arbitrarily shaped conductor encloses a charge  $q$  and is surrounded by a conducting hollow sphere as shown in the figure. Four different regions of space, 1, 2, 3 and 4 are indicated in the figure. Which one of the following statements is correct?



- (a) The electric field lines in region 2 are not affected by the position of the charge  $q$
- (b) The surface charge density on the inner wall of the hollow sphere is uniform
- (c) The surface charge density on the outer surface of the sphere is always uniform irrespective of the position of charge  $q$  in region 1
- (d) The electric field in region 2 has a radial symmetry

Ans.: (c)

Q41. Consider a small bar magnet undergoing simple harmonic motion (SHM) along the  $x$ -axis. A coil whose plane is perpendicular to the  $x$ -axis is placed such that the magnet passes in and out of it during its motion. Which one of the following statements is correct? Neglect damping effects.

- (a) Induced e.m.f. is minimum when the center of the bar magnet crosses the coil
- (b) The frequency of the induced current in the coil is half of the frequency of the SHM
- (c) Induced e.m.f. in the coil will not change with the velocity of the magnet
- (d) The sign of the e.m.f. depends on the pole (N or S) face of the magnet which enters into the coil

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Ans.: (a)

Q42. Consider a spherical dielectric material of radius 'a' centered at origin. If the polarization vector,  $\vec{P} = P_0 \hat{e}_x$ , where  $P_0$  is a constant of appropriate dimensions, then ( $\hat{e}_x, \hat{e}_y$ , and  $\hat{e}_z$  are unit vectors in Cartesian- coordinate system)

- (a) the bound volume charge density is zero.
- (b) the bound surface charge density is zero at  $(0, 0, a)$ .
- (c) the electric field is zero inside the dielectric
- (d) the sign of the surface charge density changes over the surface.

Ans.: (a), (b), (d)

Solution:  $\rho_b = -\vec{\nabla} \cdot \vec{P} = 0$

$$\sigma_b = \vec{P} \cdot \hat{n} = (P_0 \hat{x}) \cdot \hat{r} = P_0 \sin \theta \cos \phi = 0 \text{ at } (0, 0, a) \because \theta = 0.$$

Q43. For an electric dipole with moment  $\vec{P} = p_0 \hat{e}_z$  placed at the origin, ( $p_0$  is a constant of appropriate dimensions and  $\hat{e}_x, \hat{e}_y$  and  $\hat{e}_z$  are unit vectors in Cartesian coordinate system)

- (a) potential falls as  $\frac{1}{r^2}$ , where  $r$  is the distance from origin
- (b) a spherical surface centered at origin is an equipotential surface
- (c) electric flux through a spherical surface enclosing the origin is zero
- (d) radial component of  $\vec{E}$  is zero on the  $xy$ - plane.

Ans.: (a), (c), (d)

$$\text{Solution: } V_{dip}(r, \theta) = \frac{\hat{r} \cdot \vec{p}}{4\pi\epsilon_0 r^2} = \frac{p \cos \theta}{4\pi\epsilon_0 r^2}.$$

$$\vec{E}_{dip}(r, \theta) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta}).$$

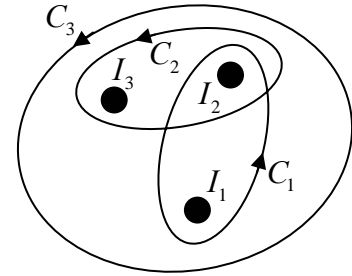
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Q44. Three infinitely-long conductors carrying currents  $I_1, I_2$  and  $I_3$  lie perpendicular to the plane of the paper as shown in the figure.



If the value of the integral  $\oint_C \vec{B} \cdot d\vec{l}$  for the loops  $C_1, C_2$  and

$C_3$  are  $2\mu_0, 4\mu_0$  and  $\mu_0$  in the units of  $\frac{N}{A}$  respectively, then

- (a)  $I_1 = 3A$  into the paper
- (b)  $I_2 = 5A$  out of the paper
- (c)  $I_3 = 0$ .
- (d)  $I_3 = 1A$  out of the paper

Ans.: (a), (b)

Solution:  $\therefore \oint_C \vec{B} \cdot d\vec{l} = \mu_0 I_{enc}$

$$\Rightarrow I_1 + I_2 = 2, I_2 + I_3 = 4, I_1 + I_2 + I_3 = 1$$

$$\Rightarrow I_1 = -3A, I_2 = 5A \text{ and } I_3 = -1A.$$

Q45. The shape of a dielectric lamina is defined by the two curves  $y=0$  and  $y=1-x^2$ . If the charge density of the lamina  $\sigma=15yC/m^2$ , then the total charge on the lamina is..... C.

Ans.: 8

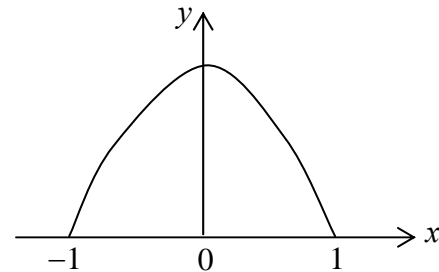
Solution: Total charge on the lamina is

$$Q = \int_S \sigma da = \int_{-1}^1 \int_0^{1-x^2} 15y dx dy = \frac{15}{2} \int_{-1}^1 (1-x^2)^2 dx$$

$$\Rightarrow Q = \frac{15}{2} \int_{-1}^1 (1+x^4 - 2x^2) dx = \frac{15}{2} \left[ x + \frac{x^5}{5} - 2\frac{x^3}{3} \right]_{-1}^1$$

$$\Rightarrow Q = \frac{15}{2} = \left[ 1 + \frac{1}{5} - \frac{2}{3} - \left( -1 - \frac{1}{5} + \frac{2}{3} \right) \right] = \frac{15}{2} \left[ 1 + \frac{1}{5} - \frac{2}{3} + 1 + \frac{1}{5} - \frac{2}{3} \right] = \frac{15}{2} \left[ 2 + \frac{2}{5} - \frac{4}{3} \right]$$

$$\Rightarrow Q = \frac{15}{2} \times \frac{16}{15} = 8 C$$



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